1. Introduction

Because of economic incentives and food security needs, West Africa is experiencing an unprecedented rapid expansion in agricultural land. Prototypical of this expansion is Burkina Faso, where natural savanna forests (SF) occupied some 60% of the land area in 1975. By 2000, this fraction dropped to 50% and presently is less than 45%. These reductions are principally due to cropland expansion, which increased from 15% in 1975 to 23% in 2000, and are currently expanding at a rate exceeding 2% per year [USGS, 2013]. The croplands are primarily fed by rainfall in this region. The southern portion of Burkina Faso is still covered by large areas of SF vegetation, but there are many growing incursions of agricultural fields (AF) into this region, which may have unintended adverse impacts on convective rainfall, the focus of this work. Specifically, using a combination of measurements and model calculations, it is shown that appreciable reductions in daytime convective rainfall due to SF to AF conversion pattern cannot be discarded. In fact, much of the total daily rainfall differences between SF and AF are primarily due to daytime differences. Data were collected in the southeastern portion of Burkina Faso over 3 years at adjacent AF and SF sites using 12 advanced weather monitoring SensorScope stations and two eddy covariance (EC) flux towers. Measured variables include sensible and latent heat fluxes by EC, mean air temperature and air humidity, shortwave and net radiation as well as precipitation measured with a network of rain gauges spatially distributed within AF and SF. The rainy season is characteristic of a Sudanian climate beginning in May and ending in October [Bagayoko et al., 2007; Ceperley et al., 2012; Mande et al., 2014]. The rainfall is short in duration, intense, and occurs mostly during daytime primarily due to convective activities [Nicholson, 2013].

2. Methods

The experiments were conducted around the village of Tambarga (11°26′42.79″N, 1°13′32.09″E), Kompienga city (see Figure 1), situated in southeastern Burkina Faso. The climate is semiarid and alternates between dry and wet seasons. These sites were selected because the savanna forest in the commune of Madjoari around the village of Tambarga covers some 70% of the adjacent area. This fractional coverage...
increases to some 90% if the surrounding Singou's basin is also included, as this aforementioned basin is
classified as protected hunting zone since 2006. However, agricultural expansion is proliferating in this
area, which is why this region was selected for the experiments here.

Two sites SF and AF, separated by more than 1500 m, were chosen for micrometeorological measurements
representing how agricultural land conversion of natural savannah may be impacting local climate in the
region. The SF is a mosaic of grassland, shrub woodlands, and dense large trees situated at an elevation of
about 100 m above the surrounding AF. The AF is a rainfed large agroforestry field used for millet and rice
plantation during the rainy season. The AF soils are loamy sand with a low permeable clay layer at a depth
about 1 m while the SF soils are shallower and are mainly sandy loam (<40 cm) mixed with a high gravel
and stone content. The SF soils do not contain a clay layer and rests directly on the sandstone parent mate-
rial. Gravel and stone content removal generally accompanies the transformation of SF to AF so as to
improve crop drainage. Meteorological data were acquired from 2009 to 2011 with SensorScope (Ss) wire-
less environmental monitoring stations and EC towers distributed over SF and the adjacent AF (Figure 1).
The Ss measures mean wind speed and direction at 2 m, air temperature, and relative humidity at 1.5 m,
precipitation intensity, incoming solar radiation at 2 m, skin temperature with radiometer positioned at
1 m, and soil moisture at different depths (0.05, 0.1, 0.2, 0.4 m). All variables were sampled or summed
every 5 min and averaged or summed every 30 min. Three Ss stations were situated within the SF and six
Ss stations were distributed within the AF to capture some of the spatial and temporal variability at each
site, especially precipitation. The EC station included a three-dimensional sonic anemometer (CSAT3, Camp-
bell Scientific, Logan UT) and an infrared gas analyzer (Licor7500, Licor, Lincoln, NE) situated at 2 m above
the ground surface along with a net radiometer (Kipp and Zonen, Delft, The Netherlands). The sampling

Figure 1. The top left map is rainfall distribution within the African continent with lightest color indicating low rainfall (100 mm yr$^{-1}$) and the dark blue color indicating the most intense rainfall (>2000 mm yr$^{-1}$). The location and topography of the Tambarga basin as well as the map of Burkina Faso are also shown. Photos of the Ss and EC stations along with the AF and SF land cover are presented for reference. The scale in the topo-map is in meters.

MANDE ET AL. CONVECTIVE RAINFALL IN SOUTHEASTERN BURKINA FASO
frequency was 20 Hz and the averaging period was 30 min for all EC variables; postprocessing utilized the planar fit technique [Pall et al., 2007] to minimize errors caused by the sonic anemometer tilt.

3. Results

To address the study objectives, the results are structured as follows. An analysis delineating the differences in precipitation between AF and SF is first presented. Next, the crossing properties between modeled lifting condensation level (using $S$) and modeled convectively grown boundary layer height (forced with the eddy covariance sensible heat flux measurements) are explored. The fractional differences in measured daytime rainfall amounts across the two sites agree with the computed differences in crossing statistics. It is shown next that deviations in crossing statistics between AF and SF are mostly attributed to differences in boundary layer dynamics that are sensitive to land cover type (mainly sensible heat) instead of lifting condensation level. A plausibility argument that differences in rainfall amounts between AF and SF is convectively driven instead of topographically induced is also presented given that the SF site is at a higher elevation than the AF (see Figure 1).

Figure 2 shows a comparison between measured cumulative daytime precipitation from all the stations at the AF and SF sites for all 3 years. Daytime is defined as the time when the sensible heat flux switched signs from negative to positive (sunrise) and from positive to negative (sunset), which almost corresponded to 6 A.M.−6 P.M. (± 15 min). Such cumulative precipitation comparison, known as the double mass analysis [Kohler, 1949], is conventionally used to assess the consistency among rainfall gages. The nighttime precipitation is not included here as the focus is on convective rainfall. Based on the measurements, daytime rain explains some 65% of the total rainfall. Figure 2 demonstrates that the rain gage network in the SF recorded a 10–30% higher daytime precipitation when compared to the AF site both for years with droughts and for wet years. These site differences are statistically significant and not connected to errors or biases in tipping bucket gage measurements because the double-mass analysis used Figure 2 shows all gages at SF recorded higher rainfall than any of the gages at AF. To place these precipitation differences in a regional context, it is noted that the measured differences in annual precipitation between AF and SF are larger than the temporal standard deviation in the 100 year annual precipitation fluctuations reported for the entire southwest Sahel [Mahé and Paturel, 2009] from 1896 to 2006 (shown in Figure 2) and exceeds all climatic change projections (in 2100) reported for the Sahel region [Hulme et al., 2001] in a doubled atmospheric CO$_2$ concentration scenario. It can be surmised from the data in Figure 2 that replacing SF with AF may lead to reduction in daytime rainfall that cannot be ignored. What is not evident from Figure 2 is the precise pathway leading to such reduction.

It has been known for some time that land cover impacts convective rainfall occurrence and amounts at local and continental scales [Kanae et al., 2001; Pielke, 2001; Findell and Eltahir, 2003; Koster et al., 2004, 2006; Santanello et al., 2007; Pielke et al., 2007; Juang et al., 2007b; Mölg et al., 2012; Bonetti et al., 2015]. Describing the initiation and amounts of convective rainfall remains a daunting scientific task [Muller et al., 2009; Tao et al., 2012], but its “predisposition” can be distilled to a minimum necessary crossing of the mixed layer height ($h$) and lifting condensation level ($H_{CC}$). This condition is necessary to ensure condensation and subsequent cloud formation but cannot be sufficient to ensure rainfall occurrences as available energy for parcels to attain the level of free convection ($>h$) and cloud condensation nuclei (CCN) must be considered at this stage. It is for this reason that the $h$-$H_{CC}$ crossing is labeled as predisposition instead of triggering for convective rainfall. The mixed layer is a region where the air column thickness ($=h$) expands due to heating from the land surface and heating caused by entrained air originating from the free troposphere. The time evolution of $h$ depends on the diurnal history of surface sensible heat flux, while the evolution of $H_{CC}$ primarily depends on the diurnal variations in mean air temperature and mean air relative humidity [Juang et al., 2007a, 2007b; Siqueira et al., 2009; De Arellano et al., 2012]. Seasonal variation in mean air temperature and relative humidity along with other synoptic scale disturbances do influence precipitation. These effects are indirectly accounted for through the calculation of $H_{CC}$. Seasonal and synoptic-scale variations govern lower atmospheric air temperature and relative humidity variations that are measured by the SensorScope stations and used to compute the diurnal variation of $H_{CC}$ as earlier noted. The minimum necessary condition of $h$ crossing $H_{CC}$ is employed here so as to assess whether replacing SF with AF explains the reductions in convective rainfall patterns using southeastern Burkina Faso as a prototypical system. It is
demonstrated that upon replacing SF by AF at spatial scales much larger than $h$ lowers $h$ but does not appreciably impact HLCL during the wet season. The suppression of sensible heat flux resulting from an SF to AF conversion leads to a reduction in the crossing probability of $h$ and HLCL. It is further shown that the reason why HLCL is not appreciably impacted by land cover is that the water vapor source within the mixed layer is not originating from the land surface during the wet season. However, sensible heat flux driving $h$ dynamics are different. Measured differences in surface water vapor fluxes are not large as these surface water vapor fluxes do not deviate appreciably from their near-wet surface evaporation values at both sites (determined by a Priestley-Taylor-type formulation). A one-dimensional slab model [Juang et al., 2007a, 2007b] coupled to an encroachment closure hypothesis linking $h$ to measured sensible heat flux time series is employed at the two sites. The slab model neglects advection and subsidence [Stull, 1988; Garcia et al., 2002; Juang et al., 2007a, 2007b] but was shown to be effective at reproducing mixed-layer heights [Pino et al., 2006; Gentine et al., 2013]. The $H_{\text{CL}}$ was estimated from diurnal variation of measured mean air temperature, air humidity, and atmospheric pressure.

Figure 3 shows atypical case of modeled $h$ and $H_{\text{CL}}$ evolution during the day using measured sensible heat flux (H) time series, and the mean air temperature and relative humidity as input (see Appendix A) at both

Figure 2. (a) Comparison of daytime cumulative precipitation between three rain gauges of the savannah forest (SF) and all combinations (i,j,k) of the rain six gauges over the agricultural field (AF). (b) Annual rainfall variability for past and future projections. Diamonds are from a long-term record for the Southwest Sahel region (1886–2006), triangles are climate model projections for the Sahel region in a doubled atmospheric CO2 scenario and for different climate models. The annual rainfall at SF (rectangle) and AF (circle) for the study sites and the experimental period are also featured.
 Shortly after the modeled $h$ intersects $H_{LCL}$, rainfall is measured by the tipping bucket gage network at both sites. When air parcels are lifted by the thermals controlling $h$ and reach $H_{LCL}$, condensation proceeds in regions of negatively buoyant overshoots within these thermals. If the overshoot kinetic energy is sufficiently large, additional lifting of condensing air parcels occurs. Latent heat is released from the lifted air parcels and their potential temperature becomes sufficiently warmer than their surrounding thereby allowing them to become positively buoyant and propelling further ascent. This height defines the so-called level of free convection, which is higher than $H_{LCL}$. The parcels may continue to rise buoyantly until they eventually become cooler than their surrounding atmosphere at which point the so-called limit of convective rise is reached. Any residual inertia in the parcels might propel them to further rise eventually terminating their ascent at the cloud top [Stull, 1988; Emanuel et al., 1994]. Once clouds develop, condensation nuclei are required to allow for rapid growth in water droplets. If these droplets reach sufficient size to precipitate and repenetrate the unsaturated air below the cloud base without completely reevaporating before reaching the ground surface, rainfall at the surface is detected. After the $h - H_{LCL}$ crossing, this entire process can be completed on time scales ranging from minutes to few hours. At SF and AF sites, when rainfall was recorded by the tipping bucket gage network, the fraction of events occurring within 3 h after the $h - H_{LCL}$ crossing exceeded 96%. There were no events in our analysis in which rainfall occurred without being preceded by an $h - H_{LCL}$ crossing. Having demonstrated that the crossing of $h$ and $H_{LCL}$ appears to be a plausible necessary condition for cloud formation and rainfall predisposition, it is now used to diagnose whether land cover explains the measured rainfall differences between AF and SF reported in Figure 2. The computed $H_{LCL}$ using measured mean air temperature and mean relative humidity are similar at both sites (Figure 4). Moreover, similarity in computed $H_{LCL}$ suggests that the external water vapor source entrained or advected into the boundary layer dictates the mean air relative humidity within $h$ at both sites, not the water vapor sources from the land surface. In fact, the latent heat (LE) fluxes measured at both sites are comparable and do not appreciably deviate from their wet surface value given by the Priestley-Taylor (PT) equation [Priestley and Taylor, 1972] with a PT coefficient of 1.26. It can be surmised from Figure 4 that land cover differences do not appreciably impact $H_{LCL}$ in the wet season here, presumably due to the weak land surface controls on the water vapor concentration within the mixed layer column. However, the measured sensible heat flux at SF is some 1.4 times larger than its counterpart at AF (Figure 4). Differences in sensible heat fluxes but similarity in latent heat fluxes suggests that either net radiation is reduced at the SF site or
soil heat fluxes must be smaller at SF when compared to AF. Figure 4 suggests that net radiation differences between AF and SF cannot explain the 1.4 increase in measured sensible heat flux. In fact, the differences in net radiation between AF and SF were not significantly different from each other. Given the constraints imposed by the energy balance, the results in Figure 4 imply that differences in sensible heat flux are likely to be due to differences in soil heat fluxes (and possible canopy storage in SF) across the two sites. Soil heat flux measurements were not conducted here primarily because of the heterogeneous rock-soil vegetation cover environment at the remote SF site. Hence, we can only offer speculations as to why large soil heat flux differences between sites exist. Several key factors influencing soil heat flux vary between the SF and AF. The forested region soils are characteristically coarser textured, and therefore better drained than those of the agricultural areas. The SF soils also have much higher proportion of rock fragments at the surface. Rocks and rock fragments are manually removed from the agricultural fields consistent with agricultural practices. While the thermal conductivity of rocks is expected to be larger than that of bulk soil, the fact that the soil is well drained in SF creates large air pockets between the rock (and its fragments) and the adjacent soil particles thereby reducing the overall thermal conductivity (and soil heat flux) of the rock-soil system. Here, the lack of soil moisture means that air gaps act as effective “insulators” to heat conduction in SF. Conversely, wetter soil moisture states in AF allow water in soil pores to act as “thermal bridges” between individual solid grain particles thereby enhancing the overall thermal conductivity of the soil-water system. Another factor impacting the differences in soil heat flux is vegetation cover. As evident from the photographs in the map figure, the AF is nearly bare during the early phases of the growing season while the soil surface in SF is reasonably covered by vegetation. Maximum leaf area index (LAI) was not
measured at the two sites; however, MODIS based maximum Net Difference Vegetation Index (NDVI) at AF was 25–30% smaller than its NDVI counterpart in SF when using MODIS pixels closest to the EC towers. While conversion from NDVI to LAI cannot be readily undertaken and is fraught with uncertainties, a lower NDVI at AF is suggestive that vegetation cover is likely to be less when compared to SF even when AF is at its maximum LAI. To summarize, while the precise cause of enhanced soil heat in AF versus SF may be debated and the aforementioned mechanism is purely speculative, the fact remains that measured daytime sensible heat is some 1.4 times larger in SF versus AF, and it is this difference that is most pertinent to convective rainfall predisposition.

Model calculations show that the excess sensible heat at SF leads to some 30% more frequent \( h - H_{\text{CL}} \) crossing, which is commensurate with the extra daytime rainfall recorded at SF when compared to AF. Moreover, the higher sensible heat flux at SF is consistent with higher probability of rainfall occurrence or yield (\( \sim 37\% \) at SF versus 23% at AF) following the \( h - H_{\text{CL}} \) crossing. Higher sensible heat flux at SF ensures that uplifted air parcels within thermal plumes have sufficient kinetic energy to become positively buoyant and be propelled to the level of free convection thereby yielding more rainfall.

It is conceivable that some of the topographic variations (see Figure 1) between SF and AF may explain the rainfall differences. This elevation difference is included in surface pressure calculations needed in \( H_{\text{CL}} \); however, the possibility of orographic lifting effects on \( h \) was not directly considered. Indirectly, an analysis on the histogram of \( S_s \) measured mean wind speeds 2 h prior to the measured rainfall occurrences was conducted. The histogram analysis suggests that these wind speeds are reasonably small (mode under 0.5 m s\(^{-1}\) in SF and in AF and more than 95% of events are below 2 m s\(^{-1}\) in SF and SF). Likewise, the histogram of EC based measured friction velocities at AF and SF 2 h prior to measured rainfall has a mode of 0.1 m s\(^{-1}\) and rarely exceeded 0.3 m s\(^{-1}\). This analysis is suggestive of (i) low mechanical production of turbulent kinetic energy driving the dynamics of \( h \) and (ii) lack of any large scale mean pressure gradient flow often associated with advection. Also, the concomitant wind direction did not exhibit any coherent spatial pattern among the SensorScope stations in SF and AF for the same periods. For SF, the most likely wind direction does not coincide with the maximum topographic gradient along the hill (data not shown). These two findings provide some (anecdotal) evidence that orographic effects impacting \( h \) or advection of moisture from one region to the other (e.g., SF to AF) is less likely. They are also consistent with the working assumption that convective processes are the dominant ones (low wind speed, variable wind direction) impacting the dynamics of \( h \) and its crossing with \( H_{\text{CL}} \).

To further explore this work assumption, scaling laws of the daytime rainfall intensity probability density function (pdf) are compared to expectations from sites dominated by summertime convective storm systems. If the daytime rainfall intensity scaling laws at the two sites appear to be commensurate with sites dominated by convective systems, then it is likely that the rainfall at both sites here originated from convective instead of orographic lifting. Figure 5 shows that the pdf of measured daytime rainfall intensity \( i \) at both sites exhibits nearly identical power-law regimes. This finding hints that the rainfall generation mechanism at the two sites must be similar; however, it does not disprove the orographic uplifting possibility. When a power law (pdf) \( f(i) = \frac{1}{i^n} \) is fitted to the rainfall data at AF and SF, an exponent \( n = 3/2 \) emerges for the range of \( i \) covered by the measurements here. This \( n \) is comparable to \( n \) reported from an 8 year record at a site dominated by summertime convective rainfall (near Durham, North Carolina, USA), also shown in Figure 5. This similarity in \( n \) across SF and AF (and other convectively dominated rainfall sites) could be used to argue against possible orographic effects as being the culprit explaining the differences in mean rainfall due to elevation differences between the AF and SF sites.

With regards to using these intensity power laws in Figure 5 for extrapolating extremes beyond the limits of the measurements, a few cautionary comments must be added. First, it did not escape our attention that when assuming a power-law intensity pdf \( f(i) \in [i_{\text{min}}, +\infty] \), the ensemble mean rainfall intensity \( \langle i \rangle \) normalized by the minimum intensity \( i_{\text{min}} \) detected by the tipping bucket gage (\( = 0.2 \text{ mm} \)) and given by \( \langle i \rangle \rangle = (i - i_{\text{min}}) / (i_{\text{min}} - i_{\text{max}}) \) is statistically divergent for \( n = 3/2 \). In practice, this mathematical divergence is unlikely to persist because the maximum intensity is bounded by finite precipitable water in the clouds. That is, physical limits on maximum precipitable water ensures that the “fat-tailed” power law in Figure 5 is “censored” thereby eliminating the divergence issue in the fitted pdf \( f(i) \). As to why \( n \) is close to \( 3/2 \) for a broad range of intensities is an interesting question recently examined in the context of convective rainfall and intermittency models [Rigby and Porporato, 2010]. It has been conjectured that some dynamical models
of intermittency are similar to convective rainfall, including the so-called Pomeau-Manneville Type-III intermittency. Such intermittency manifests a behavior intermediate between quasiperiodic and pure randomness known as “sporadic” randomness. Using the record from the Duke Forest (as used in Figure 5), it was shown that the probability distribution of laminar or quiescent phase durations and the spectrum of rainfall intensity time series are broadly consistent with a Pomeau-Manneville Type-III intermittency. However, the power-law exponent of the pdf(i) as predicted by a Pomeau-Manneville Type-III intermittency is closer to $-2$ whereas the measured pdf(i) in Figure 5 is closer to $-3/2$, an intermediate between on-off type intermittency and Type-III intermittency. This intermittency behavior may be plausible here as the dynamics of convective cells are quasideterministic in their growth and build up during the storm but are subsequently disrupted by the occurrence of rainfall (when the CCN microphysics allows it).

To summarize, similarity in measured $\alpha$ exponents across AF and SF suggests that the rainfall initiation mechanism must be similar (i.e., either both convective or both orographic). Furthermore, the fact that $\alpha = -3/2$ at both sites and agree with a reported $\alpha = -3/2$ at a site dominated by summertime convective rainfall suggests that the rainfall initiation mechanism at AF and SF is not only similar but originates from convective instead of orographic effects.

All these results support the main conjecture that daily mean rainfall at SF is larger than AF due to the more frequent crossings between ML and LCL associated with elevated sensible heat flux at SF. The impacts of orography at this site appear to be insufficient to induce the differences that are observed here.

4. Discussion and Conclusions

In water-limited areas, rainfall is the most crucial climatic parameter impacting directly the productivity and quality of life [Intergovernmental Panel on Climate Change, 2002; Pall et al., 2007]. Given the United Nations Millennium Development Goals that argue for green economic policies in Africa, understanding land cover changes and its impact on the spatial and temporal rainfall dynamics is now urgent. The effect of land cover change on precipitation pattern at larger scales has been reported in several studies [Pielke and Avissar, 1990;...
Avisar and Schmidt, 1998; Chase et al., 2001; Mölg et al., 2012; Pall et al., 2007; Pielke et al., 2007; Douglas et al., 2009). Using novel data and simplified model calculations from a data-poor region experiencing rapid land-cover change, the data-model analysis here suggests a potential impact of such land cover change on the precipitation pattern at local scales of several kilometers. Land use signature on the convective rainfall mechanism is highlighted by water vapor controlled by regional forcing while the sensible heat flux is locally controlled with a 40% difference from AF to SF. Land use change does not only include the vegetation cover but also the soil properties (e.g., plowing and the removing of stones) and subsequent consequences for water movement, drainage, and local energy balance. The local sensible heat flux enhances the likelihood of ML and LCL crossing as demonstrated here. Future research will focus on occurrences and the partitioning of extreme events at small scales and their hydrologic consequences in arid and semiarid areas. Further analysis on the coupled soil heat and moisture flow at SF (and AF) in three dimensions is clearly warranted to constrain the causes of the enhanced sensible heat flux over SF when compared to AF.

Appendix A

The ML height \( h \) was determined from a mixed-layer slab model and by adopting the encroachment closure for potential temperature \( T_p \) [Stull, 1976, 1994; Garcia et al., 2002] and by ignoring the contribution of heat sources and sinks within the ML to yield,

\[
\frac{dh}{dt} = \frac{H_s - H_t}{\rho C_p}.
\]

where \( H_s \) is the measured sensible heat flux at the surface, \( H_t \) is the entrainment flux modeled as \( H_t = -\beta h \), \( \rho \) is the mean air density, \( C_p \) is the specific heat capacity of dry air at constant pressure, and \( \gamma = g/C_p \) is the lapse rate approximated by its dry adiabatic value, \( g = 9.8 \text{ m s}^{-2} \) is the gravitational acceleration, and \( \beta \) is a constant that varies between 0.2 and 0.4, with a mean of 0.3 [Kim and Entekhabi, 1998] selected here. To solve this differential equation, an initial condition of \( h(0) = 15 \text{ m} \) was set when \( H_s \) switches from negative (night) to positive (day). For the LCL, denoted by \( H_{LCL} \),

\[
H_{LCL} = \frac{RT}{M g} \log \left( \frac{P_s}{P_{LCL}} \right),
\]

where \( R \) is the Universal gas constant (\( =8.314 \text{ J mol}^{-1} \text{ K}^{-1} \)), \( M \) is the molecular weight of dry air (\( =29 \text{ g mol}^{-1} \)), \( T \) (K) is the mean air temperature, \( P_s \) is the local surface atmospheric pressure (kPa), and \( P_{LCL} \) (kPa) can be calculated from the hydrostatic approximation,

\[
\frac{P_s}{P_{LCL}} = \left( \frac{T_{LCL}}{T} \right)^{3.5},
\]

where \( T_{LCL} \) is the saturation temperature at the \( H_{LCL} \) given by Stull [1994]

\[
T_{LCL} = 55 + \frac{2840}{3.5 \ln(T) - \ln \left( \frac{P_s}{P_{LCL}} \right)^{0.1227} - 7.108},
\]

where \( r \) is the near-surface water vapor mixing ratio derived from the measured air relative humidity. Here, the minor elevation differences between AF and SF is accounted for in \( P_s \).

References


